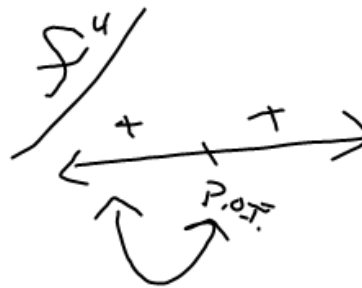
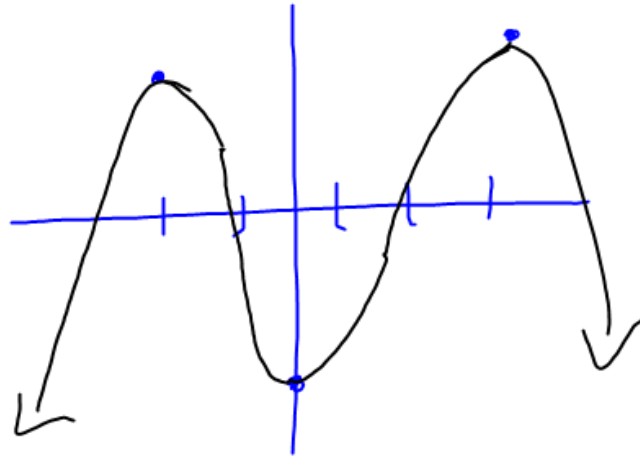
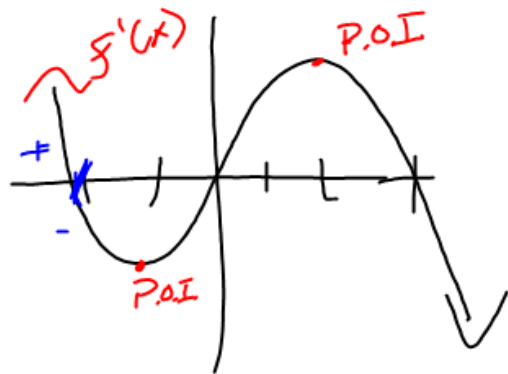


$f(x)$
 dec: $(-\infty, 2) \because x < 2$
 inc: $(2, \infty)$
 $x = 2$ Rel min





$f(x)$

inc: $(-\infty, -2) \cup (0, 3)$

dec: $(-2, 0) \cup (3, \infty)$

$x = 3, x = -2$ Rel max

$x = 0$ Rel min

$\left\{ \begin{array}{l} \text{Concave } \uparrow : (-1, 2) \\ \text{Concave } \downarrow : (-\infty, -1) \\ \phantom{\text{Concave } \downarrow : } (2, \infty) \end{array} \right.$

Pg 205

(15)_a

$$h(x) = \frac{f(x)}{x^2} = \frac{5x^3 - 3x^2 + 10}{x^2}$$

$$\lim_{x \rightarrow \infty} \frac{5x^{\textcircled{3}} - 3x^2 + 10}{x^{\textcircled{2}}}$$

DNE or ∞

①

②

③

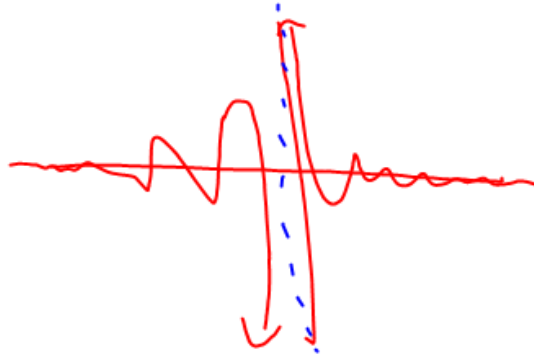
31

$$\lim_{x \rightarrow \infty} \frac{\sin 2x}{x} = 0$$

33

$$\lim_{x \rightarrow \infty} \frac{1}{2x + \sin x} = 0$$

$$\frac{1}{\infty}$$



G1

$$y = \frac{2x^2}{x^2 - 4}$$

$$y_{\text{int}}: (0, 0)$$

$$\text{VA: } x = \pm 2$$

(bottom = 0)

$$\text{HA: } y = 2$$

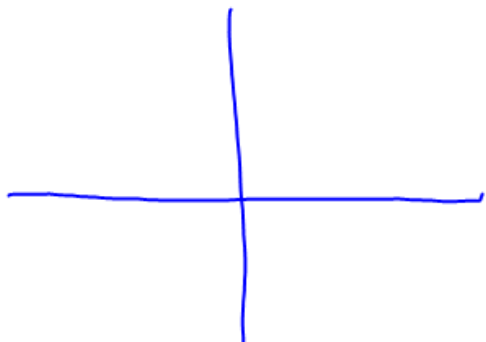
$$y' = \frac{(x^2 - 4)(4x) - 2x^2(2x)}{(x^2 - 4)^2}$$

$$y' = \frac{4x^3 - 16x - 4x^3}{(x^2 - 4)^2}$$

$$y' = \frac{-16x}{(x^2 - 4)^2}$$

$$-16x = 0$$

$$\text{C.P. } x = 0$$



3.6 Sketching

$$f(x) = \frac{2(x^2 - 9)}{(x^2 - 4)}$$

Y_{int}: $(0, \frac{9}{2})$

VA: $x = \pm 2$ (set Bottom = 0)

HA: $y = 2$ ① $\frac{x^2}{x^3} \rightarrow y = 0$

② $\frac{2x^3}{7x^3} \rightarrow y = \frac{2}{7}$

③ $\frac{x^3 - 3x^2 + 2x - 1}{x + 1} \Rightarrow y = x^2 - 2x + 4$

slant asymptote: $x + 1 \overline{) \begin{matrix} x^3 - 3x^2 + 2x - 1 \\ -x^3 + x^2 \\ \hline -2x^2 + 2x \\ +2x^2 + 2x \\ \hline 4x - 1 \end{matrix}}$

$$f'(x) = \frac{20x}{(x^2 - 4)^2}$$

C.P. $20x = 0$

Fig 215
②